

OPTIMAL INTEGRAL CONTROLLER WITH SENSOR FAILURE ACCOMMODATION

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ABSTRACT

An Optimal Integral Controller that readily accommodates Sensor Failure - without resorting to (Kalman) filter or observer generation - has been designed. The system is based on Navy-sponsored research for the control of high performance aircraft.

In conjunction with a NASA developed Numerical Optimization Code, the Integral Feedback Controller will provide optimal system response even in the case of incomplete state feedback. Hence, the need for costly replication of plant sensors is avoided since failure accommodation is effected by system software reconfiguration.

The control design has been applied to a particularly ill-behaved, third-order system. Dominant-root design in the classical sense produced an almost 100 percent overshoot for the third-order system response. An application of the newly-developed Optimal Integral Controller--assuming all state information available--produces a response with NO overshoot. A further application of the controller design--assuming a one-third sensor failure scenario--produced a slight overshoot response that still preserved the steady state time-point of the full-state feedback response.

The control design should have wide application in space systems. The design can be expanded to include gain scheduling that enhances system response to large-scale transients. For this latter instance, using the NASA optimization scheme, the guesswork normally required to determine feedback gains for large transients is eliminated.

Optimal Integral Control
With
Sensor Failure Accommodations

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N A S A Workshop
Flexible System Control
12 July 1988

1005

Optimal Integral

Control Design

Introduction

Optimal Regulator

Augmented System

(Rates of Change of Input Signals)

Optimal Tracker

Optimal Integral

Control Design

Sensor Failure

Accommodation

Preliminary Results:

Third Order System

1006

Introduction

Optimal Control Designs Compromised By:

Inaccessible States (Sensors)

Noisy Feed back Signals

OC Designs Resort To Use Of

Filter / Estimating Techniques

To Overcome These Obstacles

NAVY Research in 1970s

Leads to Alternative Approach

1007

Optimal Regulator - Classic Design
Tradeoffs Between Accuracy of Control
And Energy Expenditure Reflected
In Weighting Matrices (Q and R)
Of Performance Index (J)

$$J = \int (X^T Q X + U^T R U) dt$$

Performance Index Formulation
Assumes Unconstrained Inputs.
In Reality, Inputs are Limited.
Furthermore, Rates of Change of
Input Signals Are Limited.

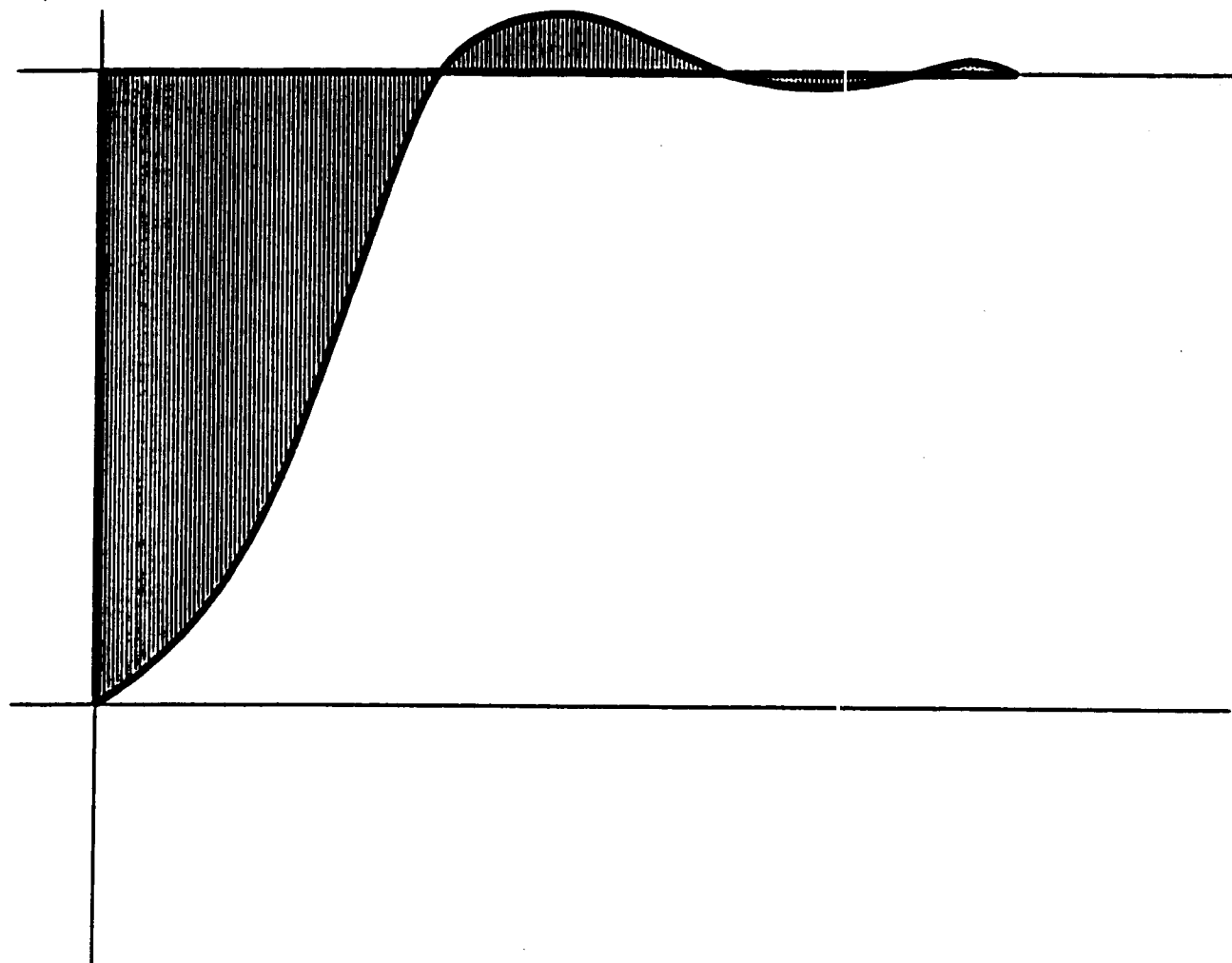


Figure 1. Typical System Response.

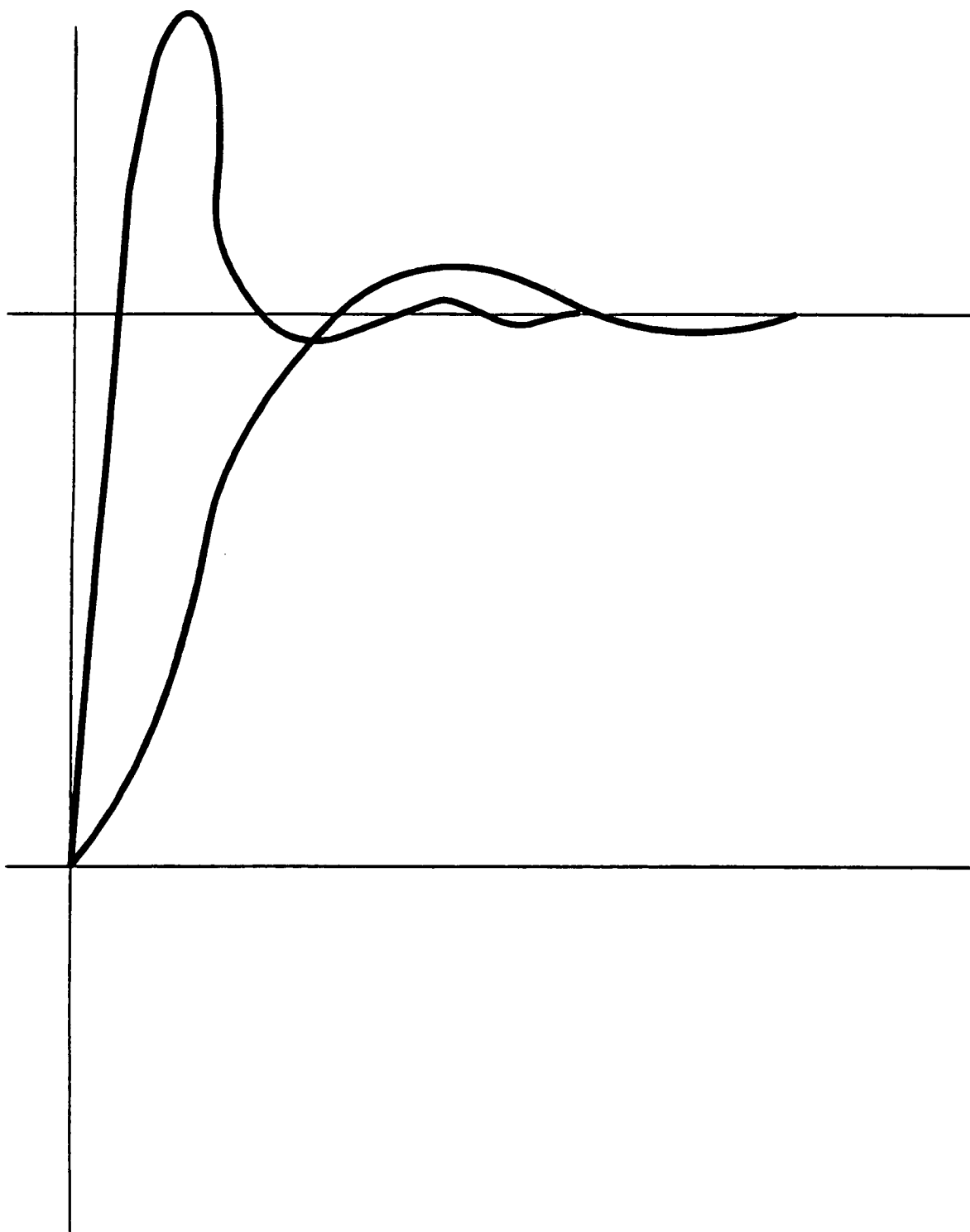


Figure 2. Comparative Optimal Responses.

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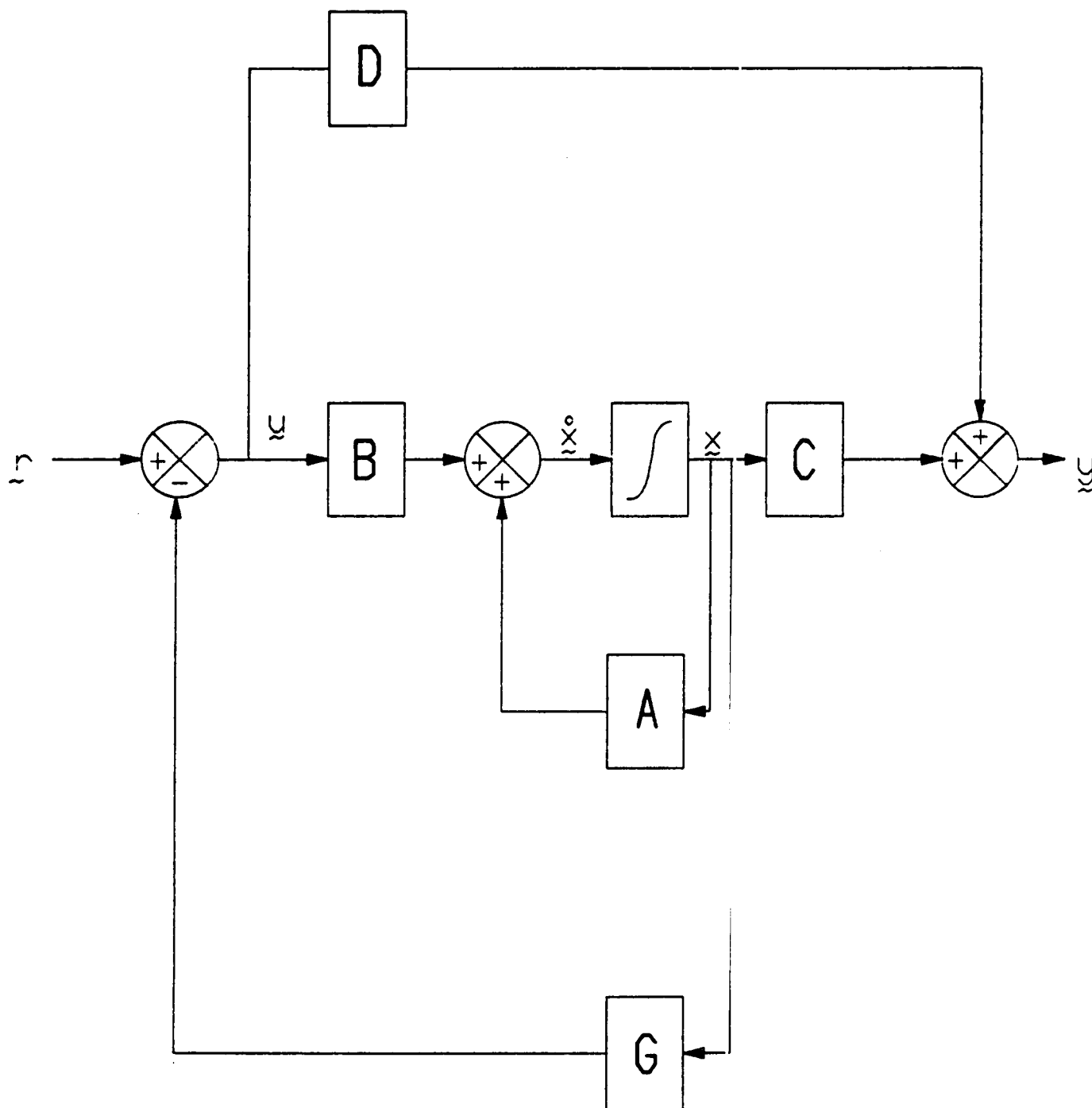


FIGURE 3. OPTIMAL REGULATOR SYSTEM

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Augmented System:

Rates of Change of Input Signals

Can be Considered

**New State Vector = Old State Vector
+
Input Signals**

Optimal Regulator Solution of

Augmented System:

$$\mathbf{U}^* = -\mathbf{G}^* \mathbf{X}^* \quad \mathbf{G}^* = [\mathbf{G}_1 \quad \mathbf{G}_2]$$

Gain Matrix (\mathbf{G}^*) of Augmented

System Carries Information on System

States (\mathbf{X}) and Inputs (\mathbf{U})!

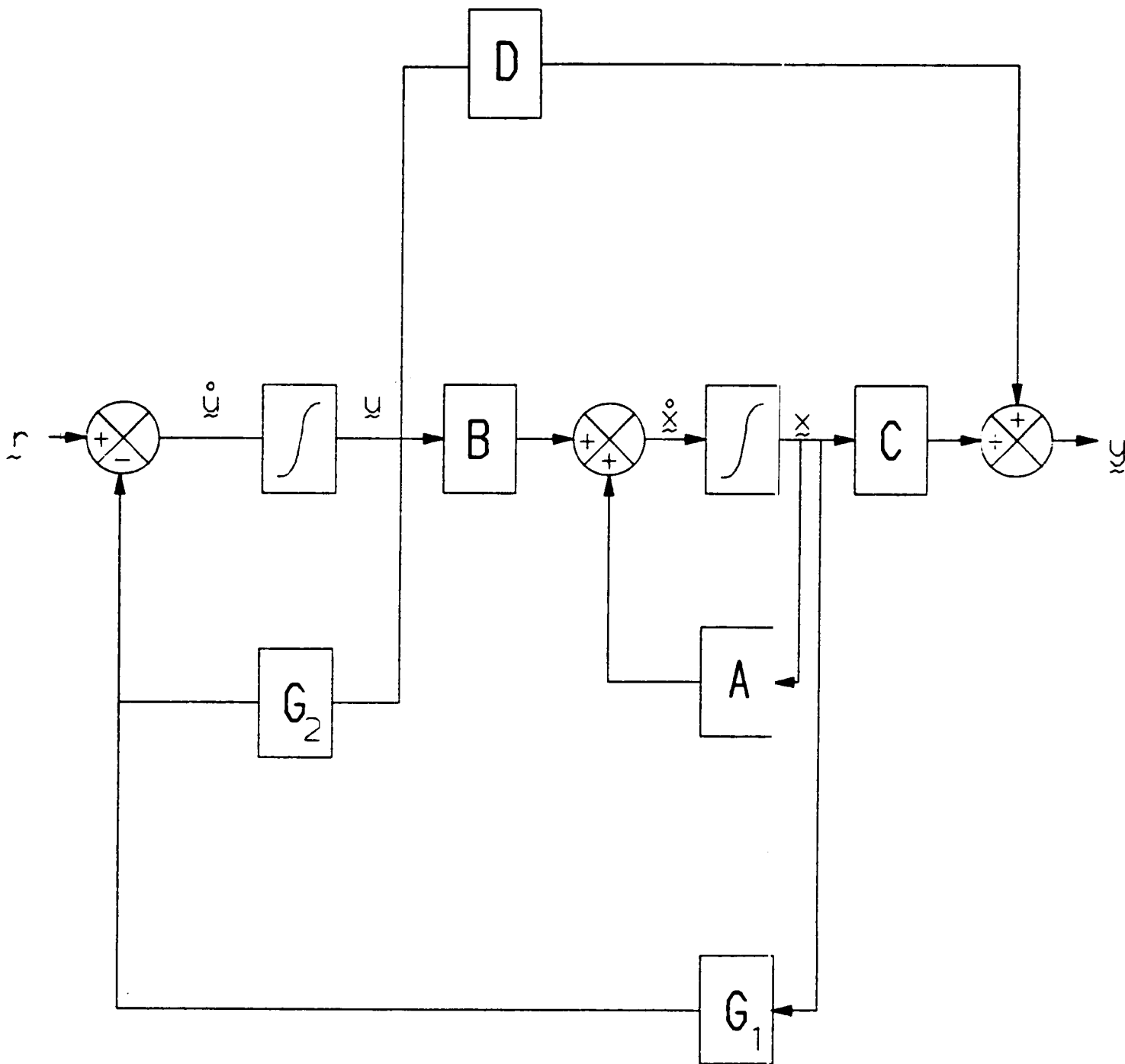


FIGURE 4. OPTIMAL REGULATOR-AUGMENTED SYSTEM

1013

Optimal Tracker:

Add Gain Matrix (M) to

Select Command Inputs

NOTE: Tracker is NOT Integral Controller

Since Control Commands are NOT

Generated by Integral of Error

Between Desired Signals (r)

And Output Signals (z).

NOTE: Solution to Tracker Control

Configuration is KNOWN. It is

Solution of Augmented System.

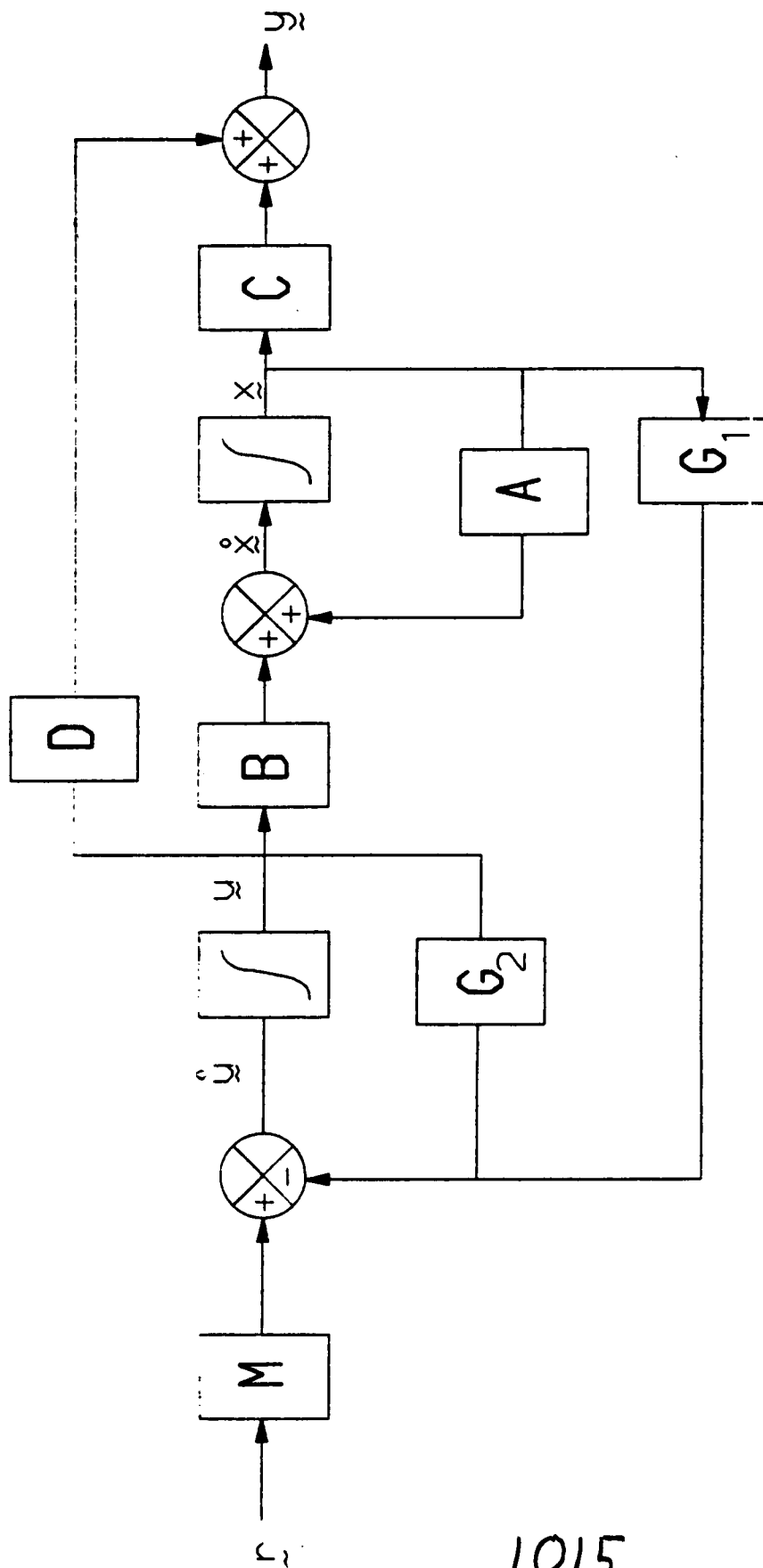


FIGURE 5. OPTIMAL TRACKING SYSTEM

Optimal Integral Control Design

Equality of Optimal Integral Control

Design and Optimal Tracker Design

Effected by Block Diagram Reduction

Techniques (Laplace Domain).

Results:

$$|L H| = |G_1 G_2| \begin{vmatrix} A & B \\ EC & ED \end{vmatrix}^{-1}$$

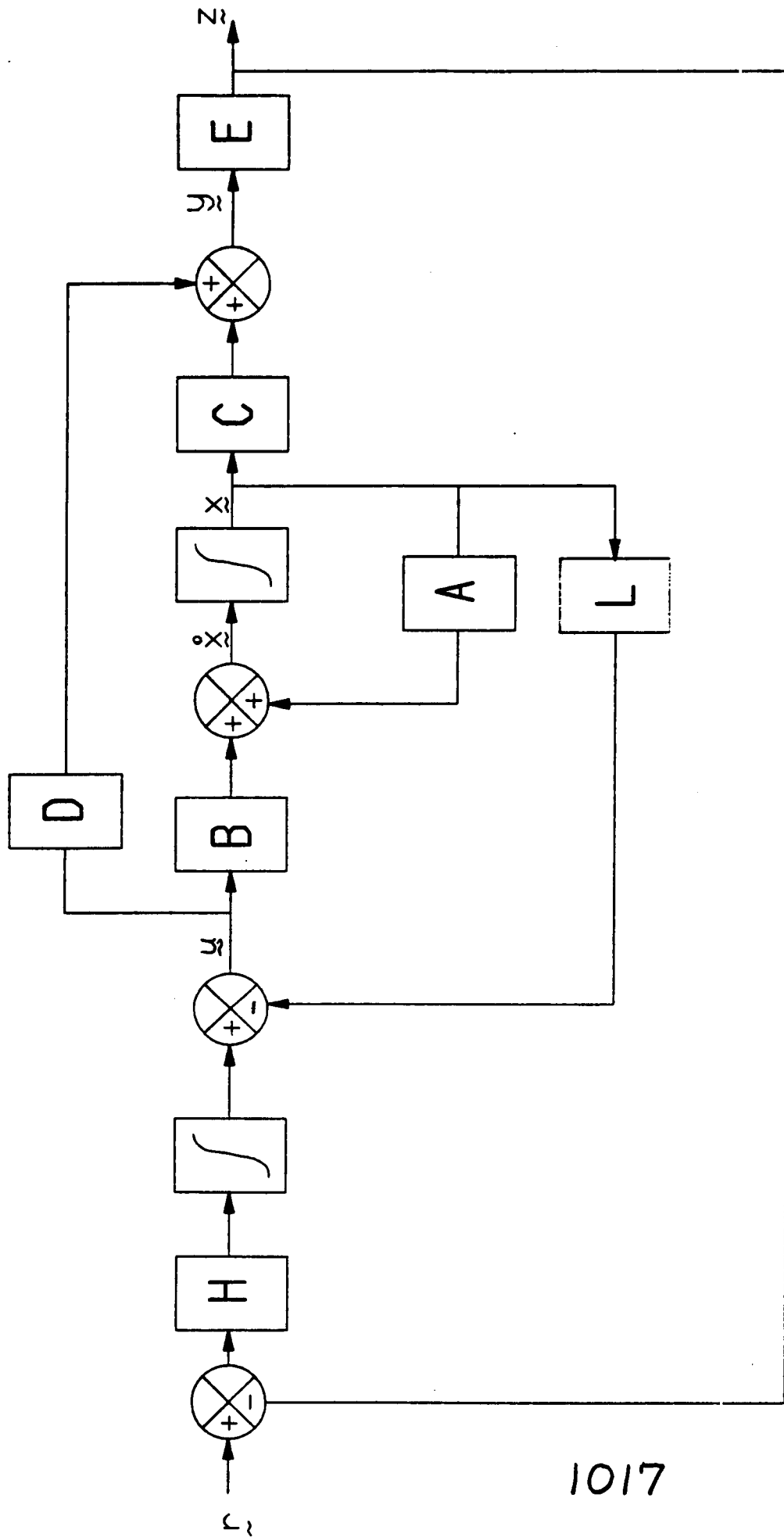
Knowns:

A, B, C, D, E - Configuration Matrices

G₁, G₂ - Augmented System Solution

Thus:

L and H Matrices are Determinable



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FIGURE 6. OPTIMAL INTEGRAL TRACKING SYSTEM

Sensor Failure Accommodation

Matrices:

H = Error Gain Matrix

L = State Gain Matrix

If State Information Unavailable,

Corresponding Column Elements of L

Matrix Are Zeroed - Suboptimal Control!
From Before

$$|G_1 G_2| = |L_s H| \begin{vmatrix} A & B \\ EC & ED \end{vmatrix}$$

Hence, New Gain Matrix $|G_s| = |G_{1s} G_{2s}|$

Can be Determined to Effect Control

Preliminary Results are Encouraging

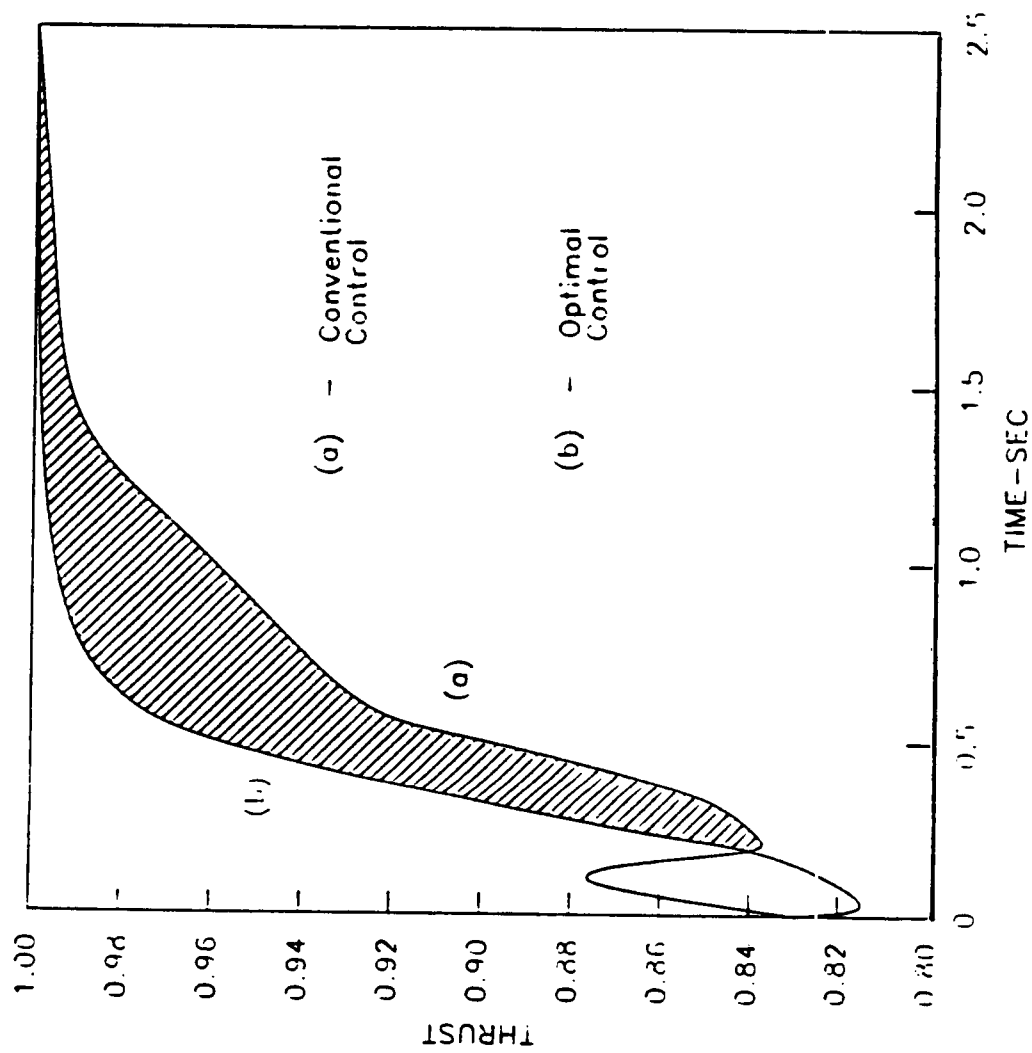


FIG. 7 F-100 THRUST CONTROL

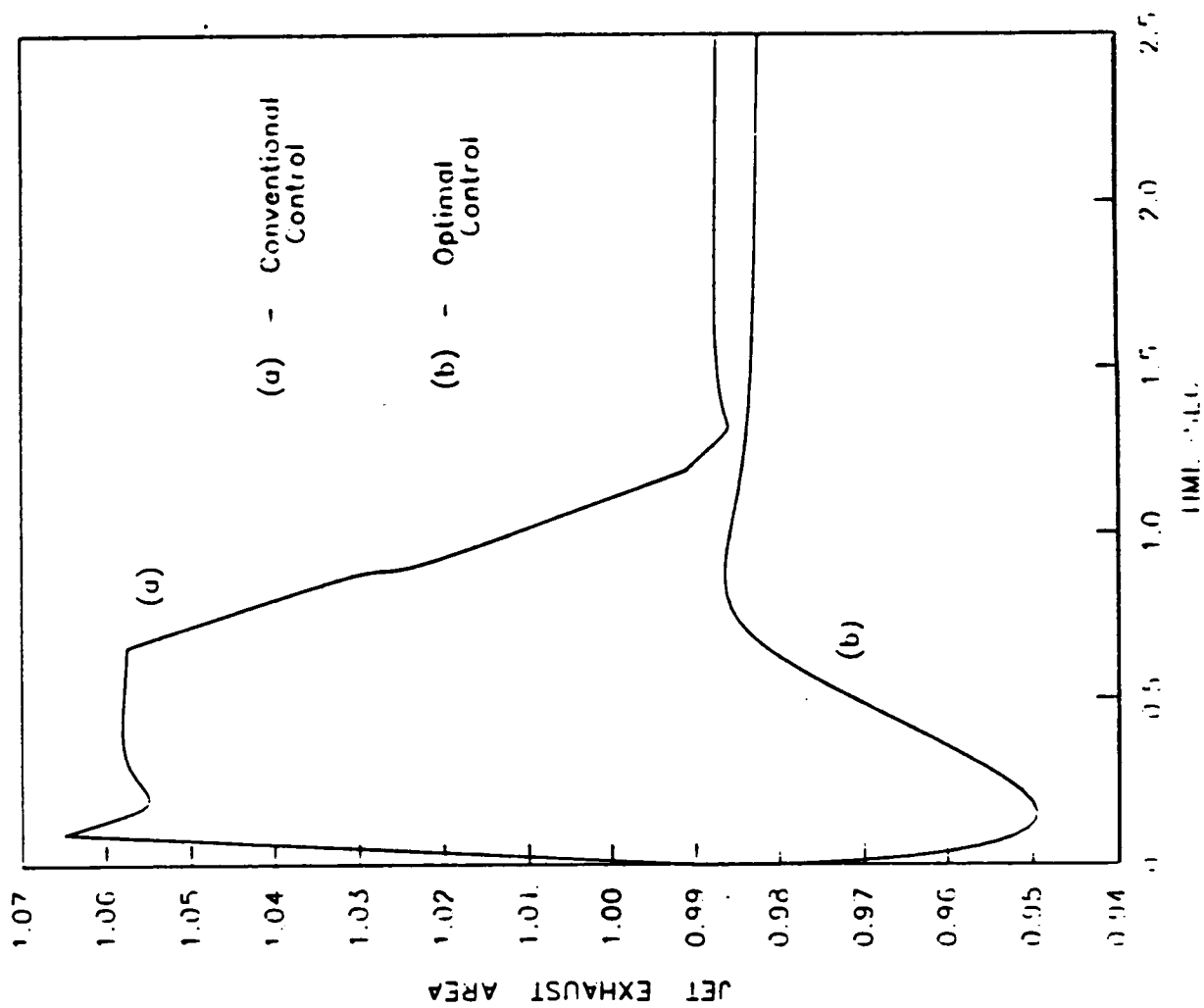


FIG. 8 F-100 AFTERBURNER CONTROL

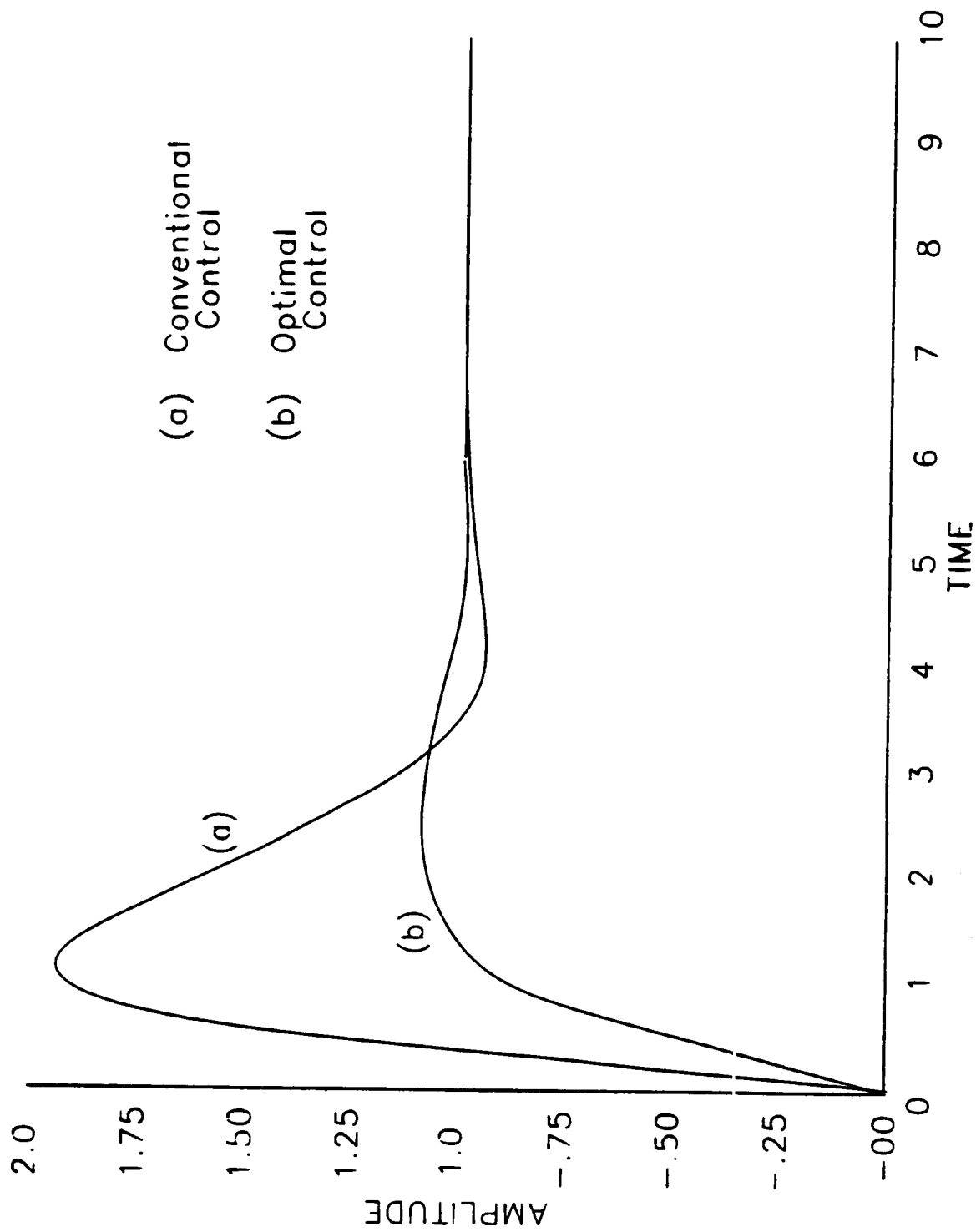


Fig.9. Third Order System Response Comparison

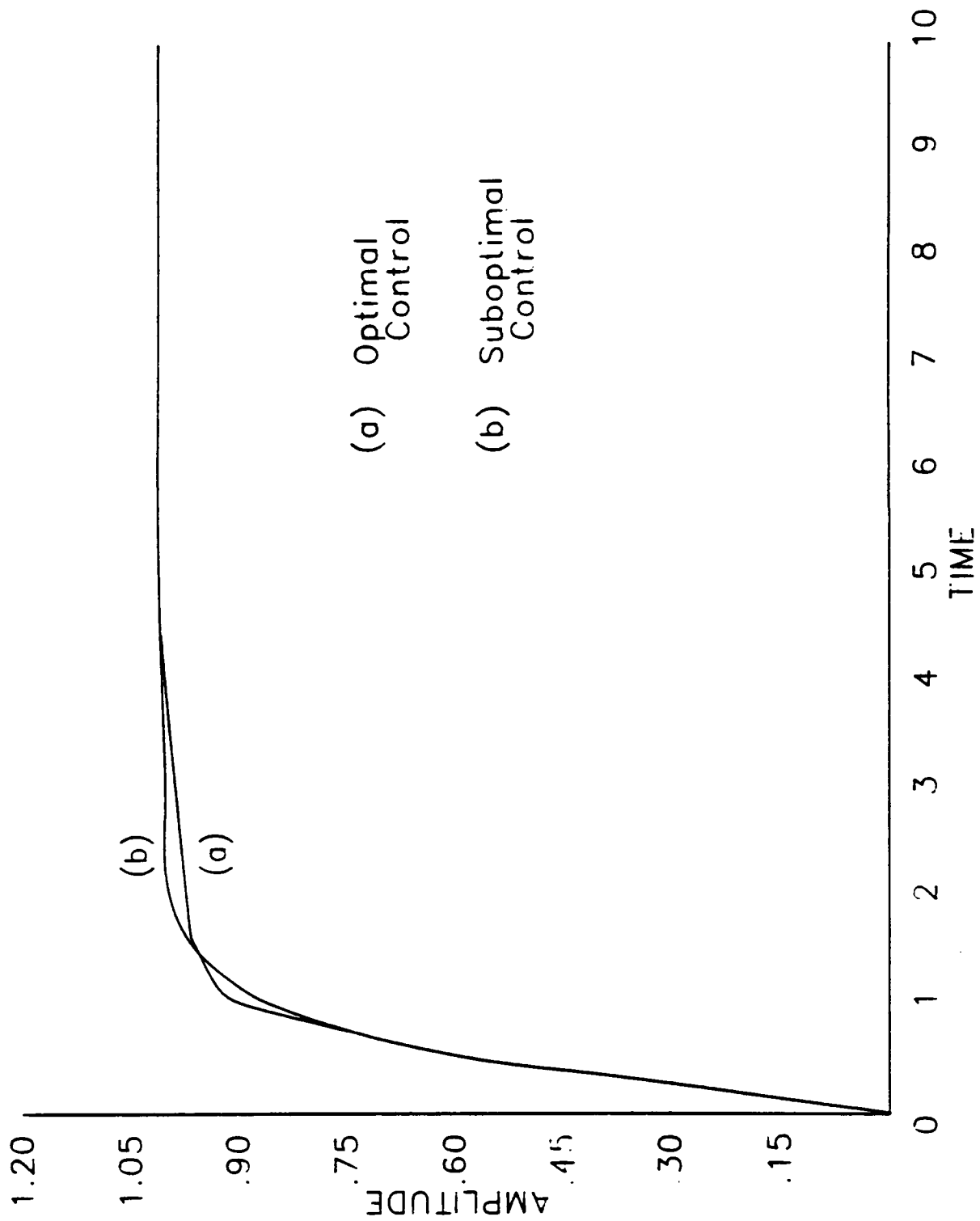


Fig.10. Third Order System Response Comparison

Summary

**Optimal Integral Control Design
Effected by a Combination of
Multivariable Control Analyses**

**Sensor Failure Accommodation
Accomplished Without Resort to
Supplemental Filter / Estimator Designs**

**Suboptimal Control Response
Effective for Ill-Behaved,
Third-Order Test Case**

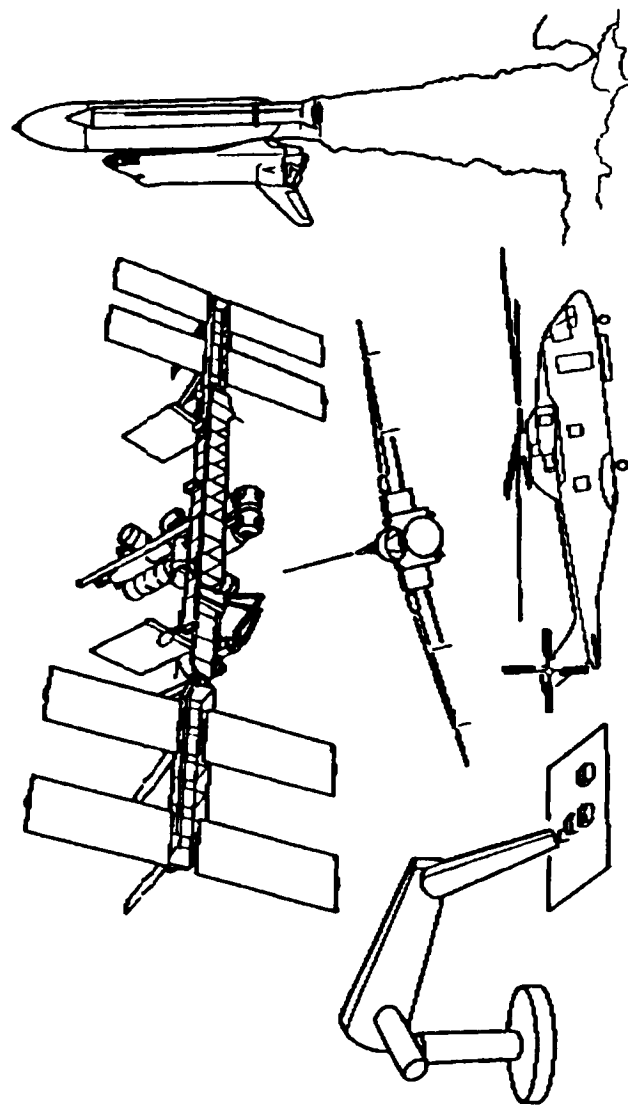
Postscript to Computational Aspects...

Lawrence W. Taylor, Jr.
NASA Langley Research Center

What started as an effort to transcend various project and reasearch activities has become an official program..Computational Controls. The following charts describes that program at this early stage in its development. The next meeting on the subjects of the Computational Aspects Workshop will be the 3rd Annual Conference on Aerospace Computational Control. The conference will be held August 28-30, 1989 at Oxnard.

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Computational Controls

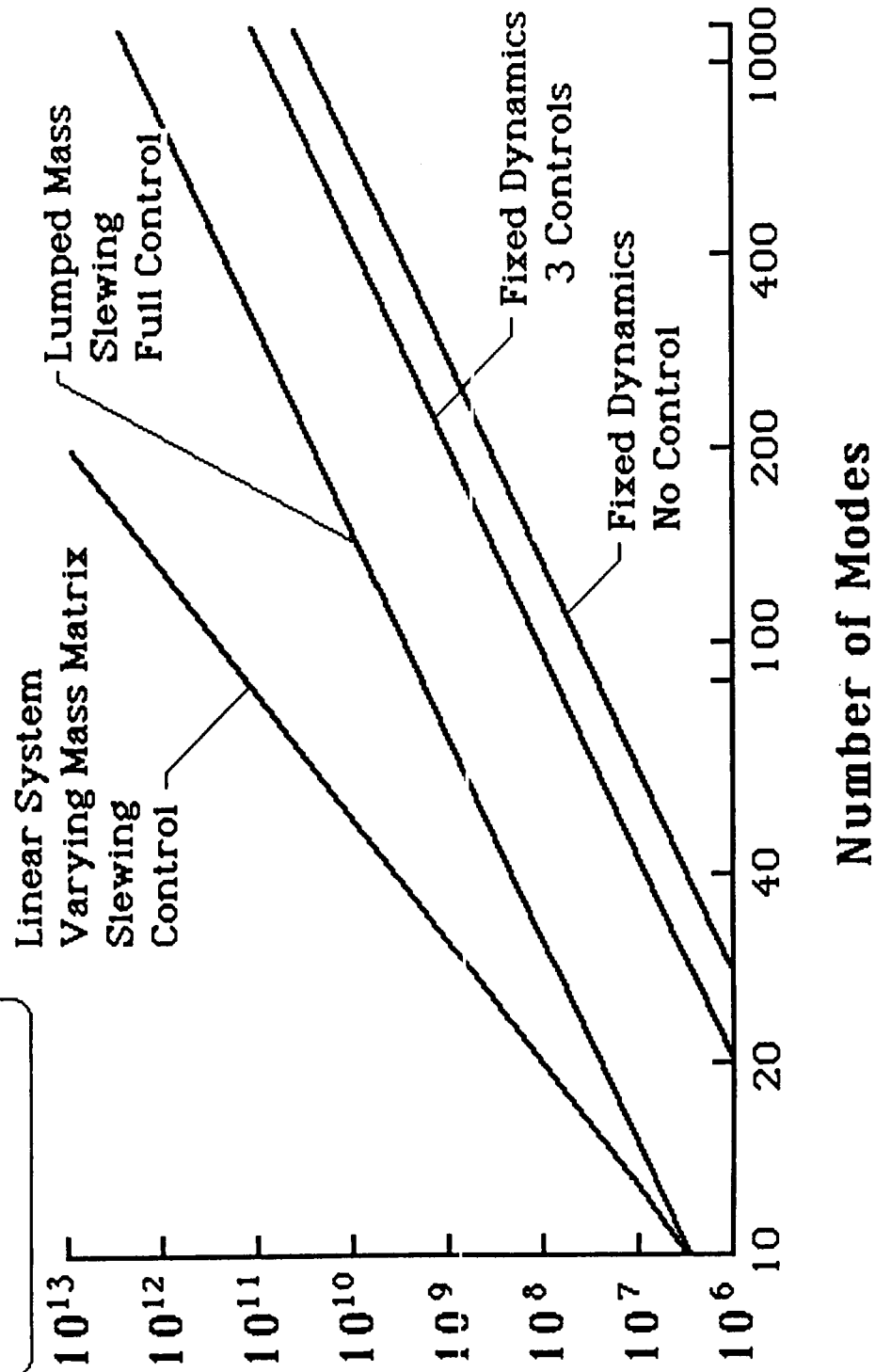


Larry Taylor
NASA Langley Research Center

Computational Requirements

Multiplies
per P_1

Planar Beam Example



Computational Controls

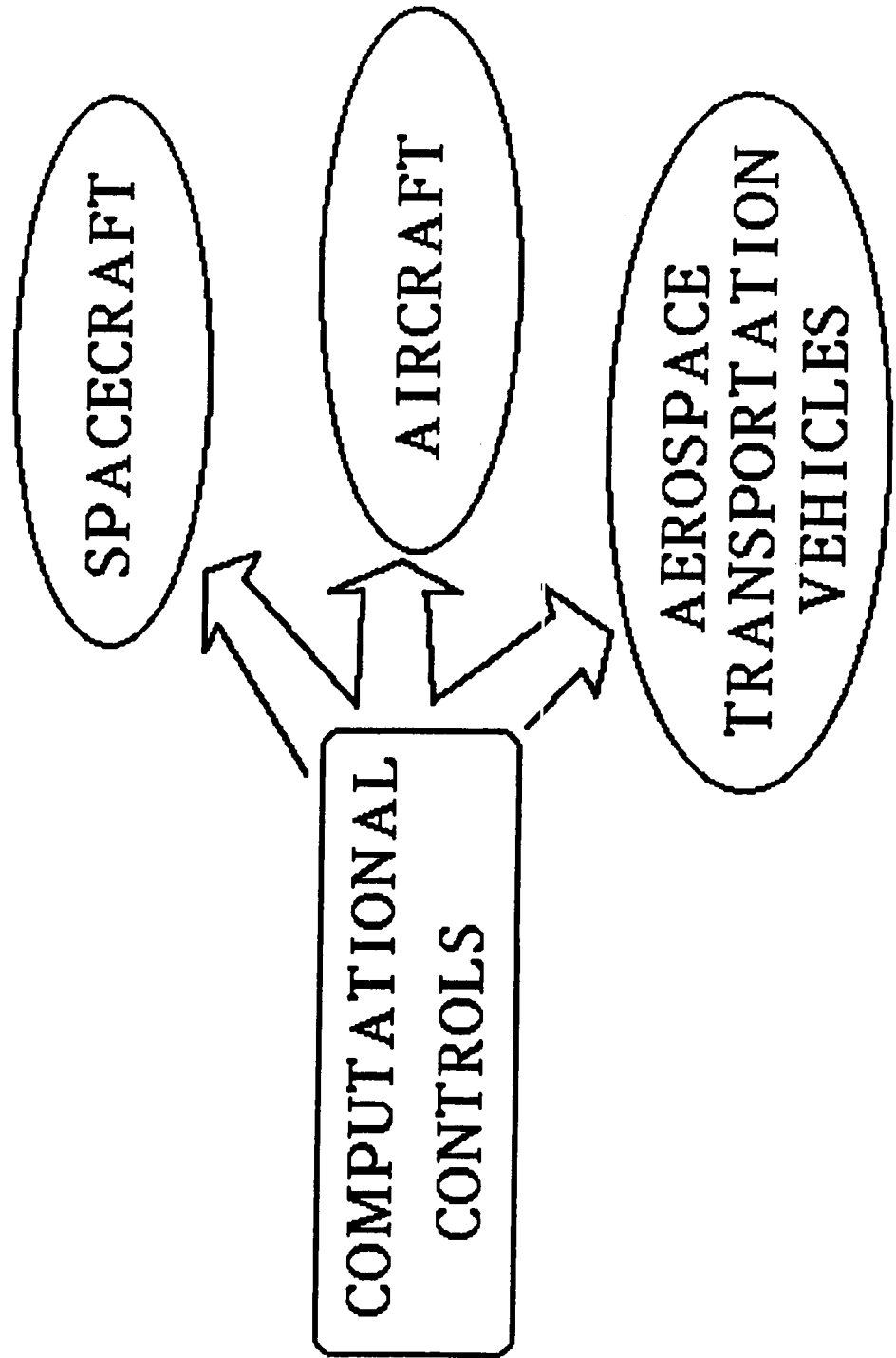
OBJECTIVE

"To Develop the NEW GENERATION

HIGH PERFORMANCE Aerospace

Modeling, Control, and Simulation Tools"

A THREE-PART PROGRAM



Computational Controls

Contacts:

Lee Holcomb - NASA HQ Code RC

John Dibattista - NASA HQ Code RC

Guy Man - JPL

Larry Taylor - LaRC

Harry Frisch - GSC

Henry Waites - MSFC

Ken Cox - JSC

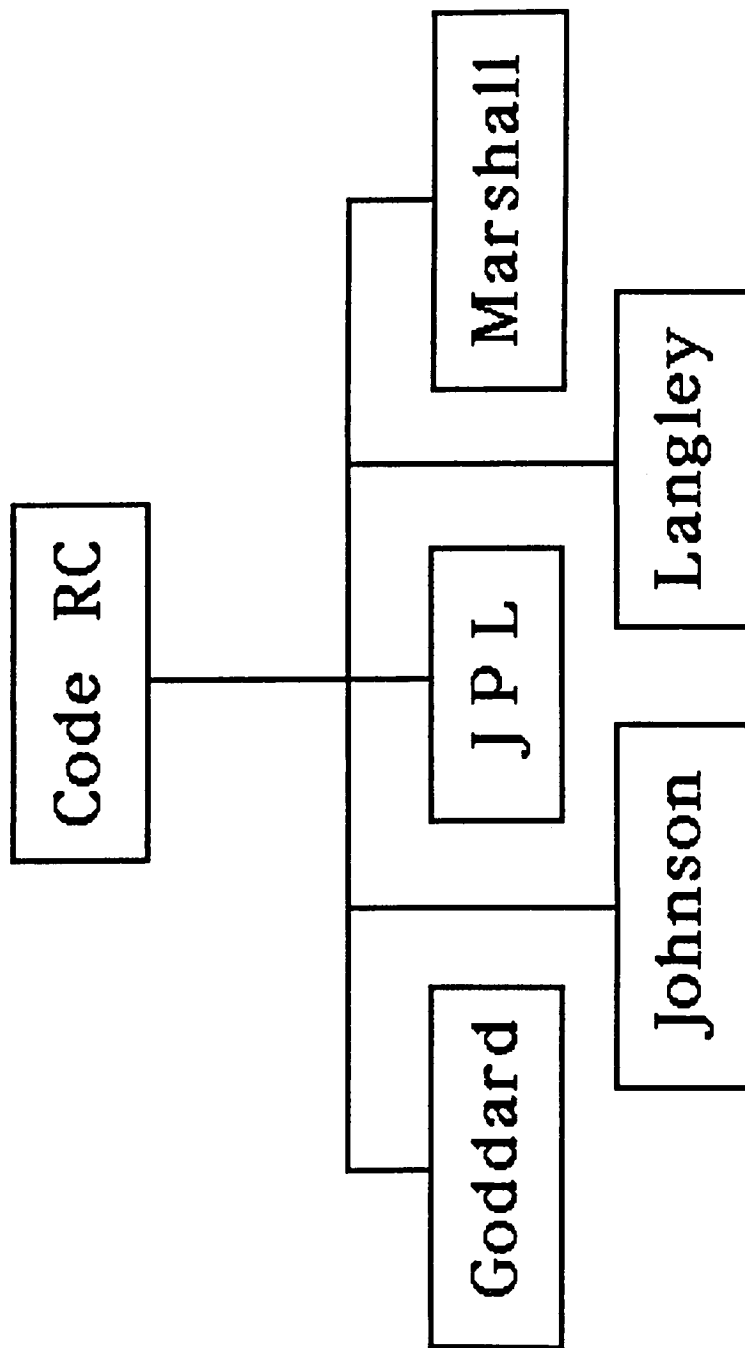
JUSTIFICATION

Current Practices in Formulating,
Modeling and Simulating do not

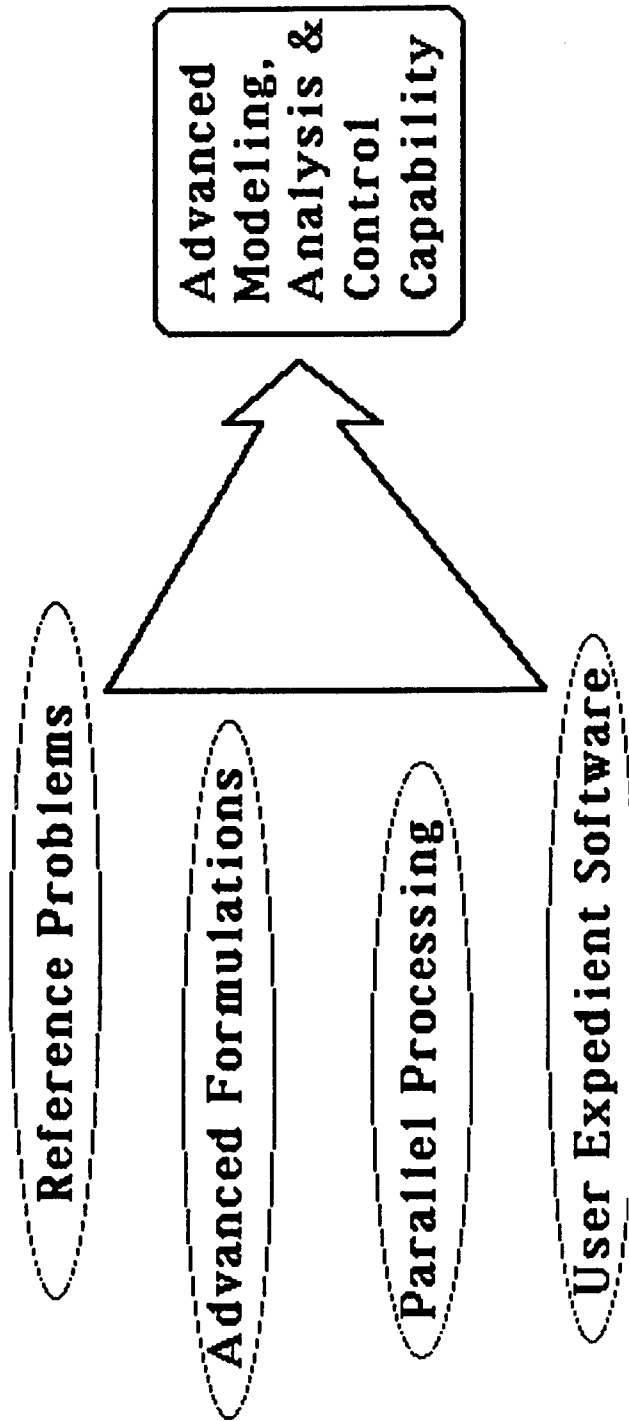
Meet today's needs.

- Hypersonic Cruise Vehicles
- Multi-Component Launch Vehicles
- Aeroassisted Orbital Transfer Vehicles

ORGANIZATION



APPROACH



Reference Problems

- Shuttle RMS
- Earth Orbiting Satellite
- Mini-MAST
- Pinhole Occulter
- Mariner Mark II
- Optical Interferometer
- Advanced Launch System
- F - 18 Fighter
- Trans-Atmospheric Vehicle

Advanced Formulations

- Order(n) Algorithms LaRC
- Distributed Parameter Modeling LaRC
- Mass Referenced Modeling LaRC
- Composite Modeling LaRC

Parallel Processing

- Multiple Processors
- Array Processors
- Benchmarking

LaRC

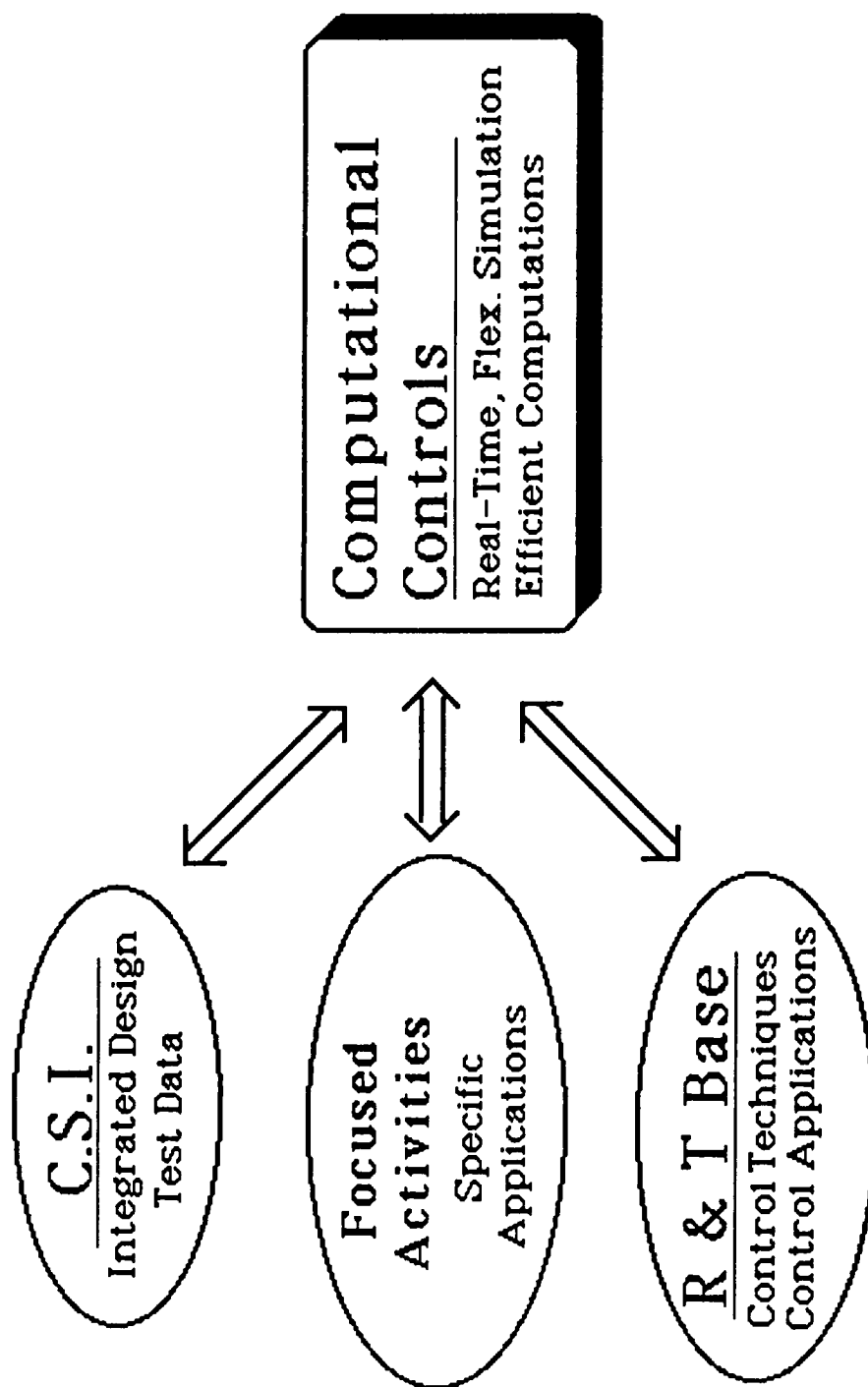
LaRC

LaRC

SOFTWARE

- Macintosh-Like User Environment
- Simultaneous Tasking
- Real-Time and Off-Line
- Modular (Particular Methods) LaRC
- Data Base Management
- Interactive Graphics

Related Activities



PROPOSED LARC AERO TASKS

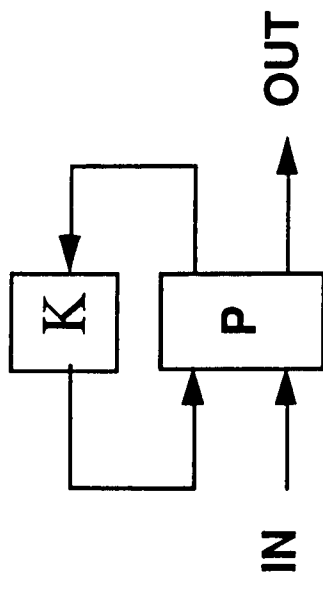
1.1

DYNAMICS INTEGRATION AND ADVANCED CONTROL THEORY AND MODELING

- F-18 THRUST VECTORED HI- α VERSION
- TRANS-ATMOSPHERIC

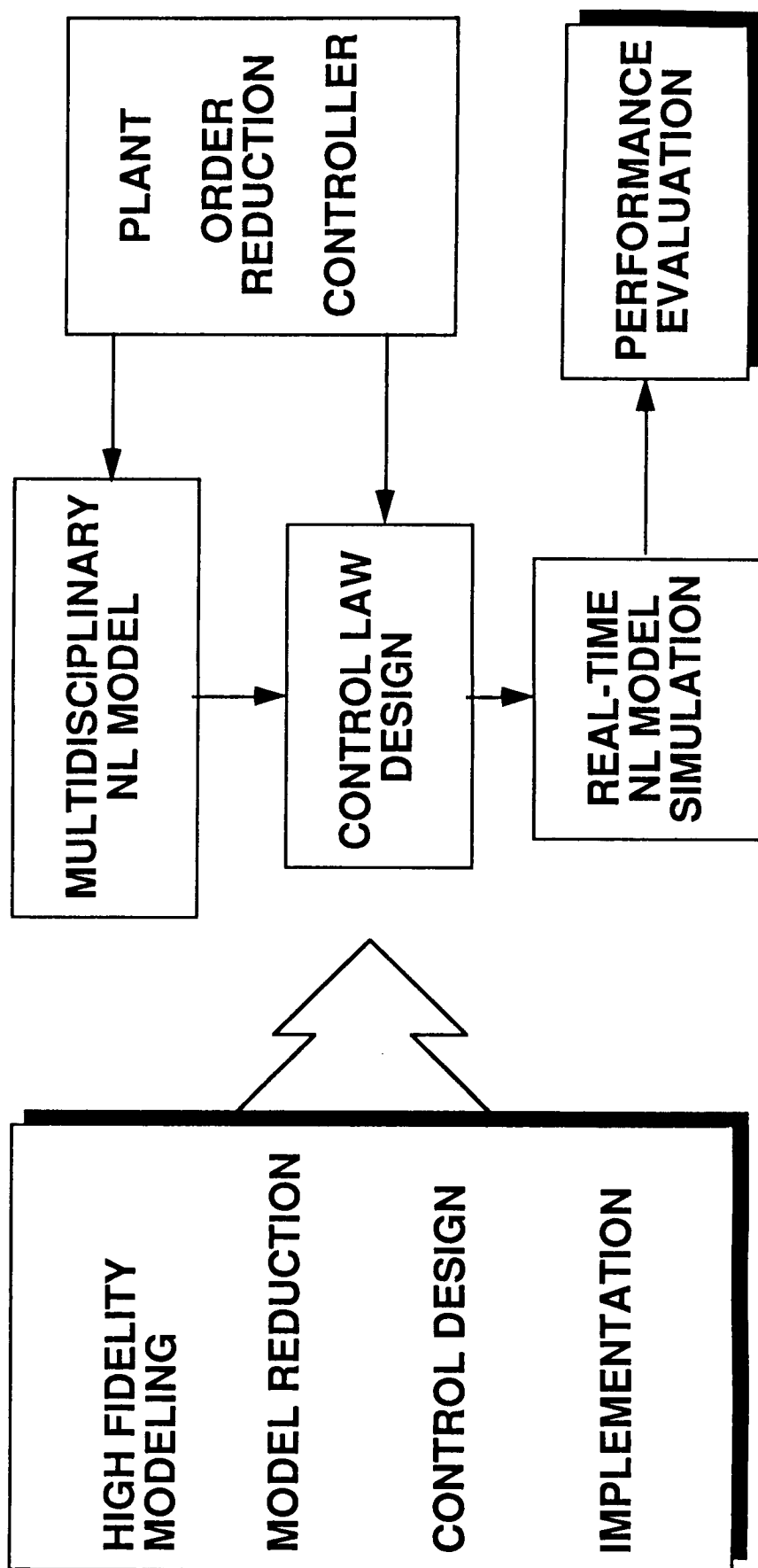
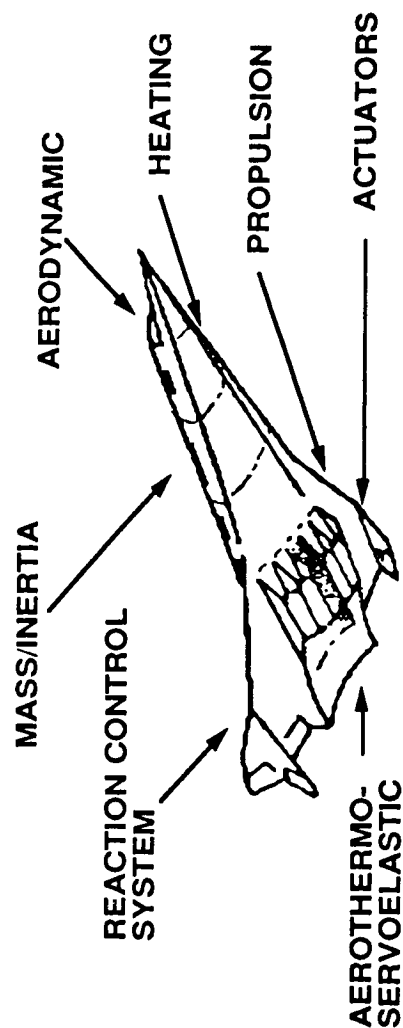
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HIGH-ORDER, HIGH FIDELITY, NONLINEAR
MATHEMATICAL MODELS OF HIGH PERFORMANCE AIRCRAFT
ADVANCED MODEL ORDER REDUCTION METHODS
ROBUST INTEGRATED CONTROL DESIGN METHODOLOGIES

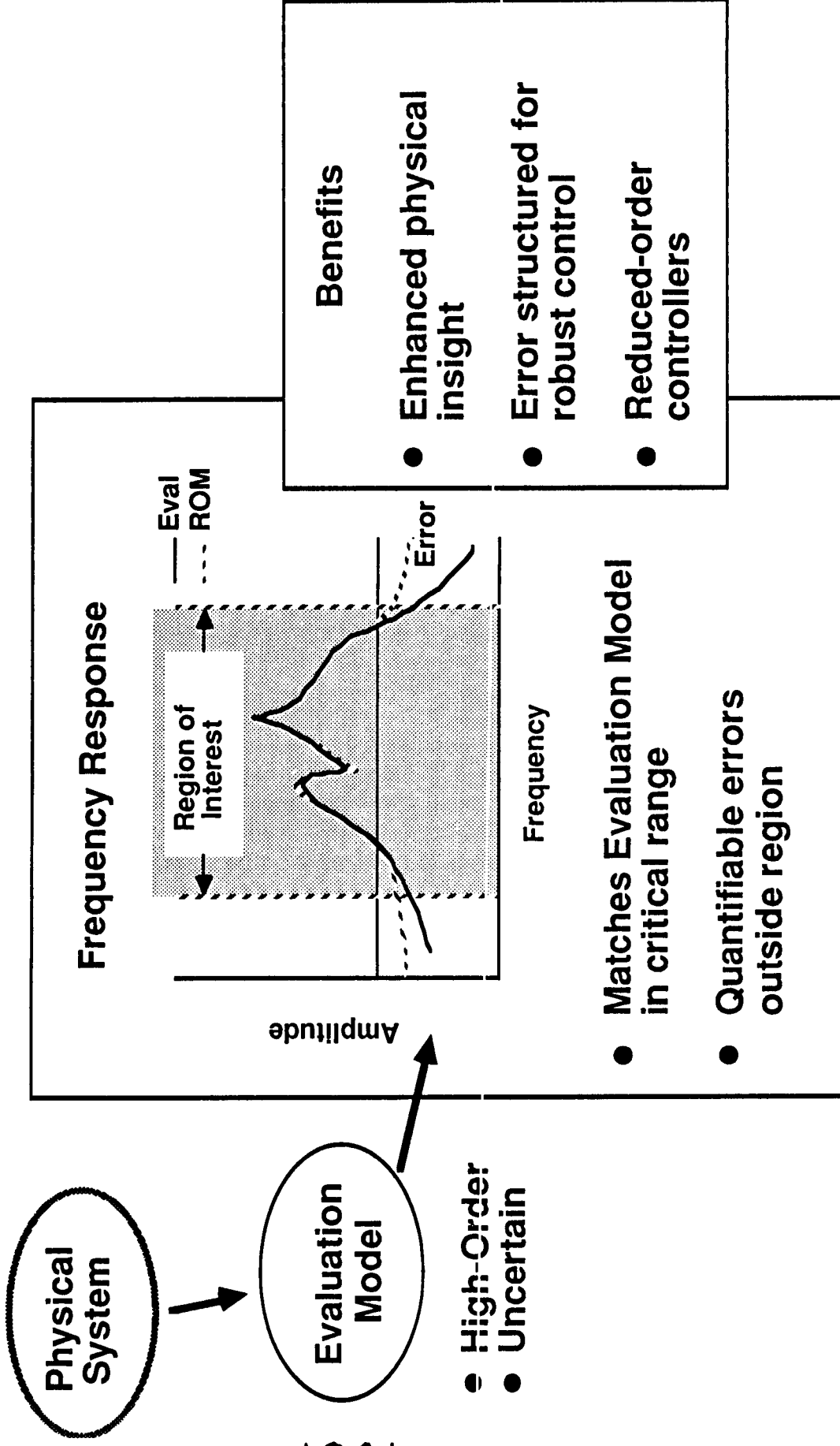


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RAPID CONTROLLER IMPLEMENTATION METHODOLOGIES



Plant Order Reduction for Controller Synthesis



ACTIVITIES

- Advisory Committee /Quarterly
- Workshops /Annually
- Programmatic Status Repts /Quarterly
- Technical Reports /As Available

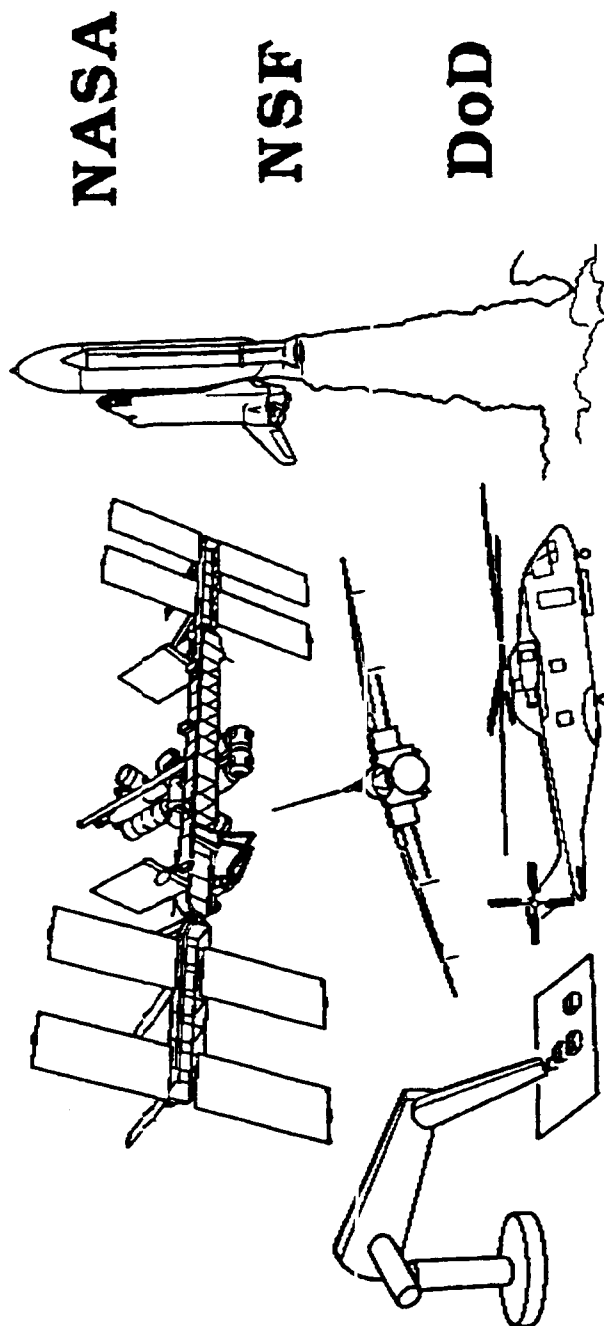
ANNOUNCEMENT & CALL FOR PAPERS

3rd Annual Conference on Aerospace Computational Control

Radisson Suite Hotel

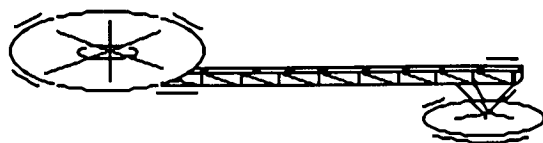
August 28-30, 1989

Oxnard, California



ANNOUNCEMENT of a CLASS on

TREETOPS*



* A Control System Simulation for
Flexible and Articulating Structures

WHEN: August 31, 1989(After Conference)

WHERE: 3rd Annual Conference on
Aerospace Computational Control
Radisson Suite Hotel, Oxnard, CA

CONTENT:

- Overview
- Example Problems
- Hands-On Experience
- User's Manual

COST: No Charge for Class or Materials
for Registered Conferees

CLASS REGISTRATION: Larry Taylor
NASA Langley
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